

## Trig Identity Table

$e^{\pm j\theta} = \cos(\theta) \pm j \sin(\theta)$
$\cos(\theta) = \frac{e^{j\theta} + e^{-j\theta}}{2}$
$\sin(\theta) = \frac{e^{j\theta} - e^{-j\theta}}{2j}$
$\cos(\theta \pm \pi/2) = \mp \sin(\theta)$
$\sin(\theta \pm \pi/2) = \pm \cos(\theta)$
$2 \sin(\theta) \cos(\theta) = \sin(2\theta)$
$\sin^2(\theta) + \cos^2(\theta) = 1$
$\cos^2(\theta) - \sin^2(\theta) = \cos(2\theta)$
$\cos^2(\theta) = \frac{1}{2}[1 + \cos(2\theta)]$
$\sin^2(\theta) = \frac{1}{2}[1 - \cos(2\theta)]$
$\cos^3(\theta) = \frac{1}{4}[3\cos(\theta) + \cos(3\theta)]$
$\sin^3(\theta) = \frac{1}{4}[3\sin(\theta) - \sin(3\theta)]$
$\sin(A \pm B) = \sin(A)\cos(B) \pm \cos(A)\sin(B)$
$\cos(A \pm B) = \cos(A)\cos(B) \mp \sin(A)\sin(B)$
$\sin(A)\sin(B) = \frac{1}{2}[\cos(A - B) - \cos(A + B)]$
$\cos(A)\cos(B) = \frac{1}{2}[\cos(A - B) + \cos(A + B)]$
$\sin(A)\cos(B) = \frac{1}{2}[\sin(A - B) + \sin(A + B)]$
$a \cos(\theta) + b \sin(\theta) = C \cos(\theta + \phi)$
$C = \sqrt{a^2 + b^2} \quad \phi = \tan^{-1}(-b/a)$

## Integral Table

$\int u dv = uv - \int v du$
$\int f(x)g'(x)dx = f(x)g(x) - \int f'(x)g(x)dx$
$\int \sin(ax)dx = -\frac{1}{a}\cos(ax)$
$\int \cos(ax)dx = \frac{1}{a}\sin(ax)$
$\int \sin^2(ax)dx = \frac{x}{2} - \frac{1}{4a}\sin(2ax)$
$\int \cos^2(ax)dx = \frac{x}{2} + \frac{1}{4a}\sin(2ax)$
$\int x \sin(ax)dx = \frac{1}{a^2}[\sin(ax) - ax \cos(ax)]$
$\int x \cos(ax)dx = \frac{1}{a^2}[\cos(ax) + ax \sin(ax)]$
$\int x^2 \sin(ax)dx = \frac{1}{a^3}[2ax \sin(ax) + 2 \cos(ax) - a^2 x^2 \cos(ax)]$
$\int x^2 \cos(ax)dx = \frac{1}{a^3}[2ax \cos(ax) - 2 \sin(ax) + a^2 x^2 \sin(ax)]$
$\int \sin(ax) \sin(bx)dx = \frac{1}{2(a-b)}\sin((a-b)x) - \frac{1}{2(a+b)}\sin((a+b)x)$ $a^2 \neq b^2$
$\int \sin(ax) \cos(bx)dx = -\frac{1}{2(a-b)}\cos((a-b)x) - \frac{1}{2(a+b)}\cos((a+b)x)$ $a^2 \neq b^2$
$\int \cos(ax) \cos(bx)dx = \frac{1}{2(a-b)}\sin((a-b)x) + \frac{1}{2(a+b)}\sin((a+b)x)$ $a^2 \neq b^2$
$\int e^{ax} dx = \frac{1}{a}e^{ax}$
$\int x e^{ax} dx = \frac{1}{a^2}e^{ax}(ax - 1)$
$\int x^2 e^{ax} dx = \frac{1}{a^3}e^{ax}(a^2 x^2 - 2ax + 2)$
$\int e^{ax} \sin(bx)dx = \frac{1}{a^2 + b^2}e^{ax}(a \sin(bx) - b \cos(bx))$
$\int e^{ax} \cos(bx)dx = \frac{1}{a^2 + b^2}e^{ax}(a \cos(bx) + b \sin(bx))$